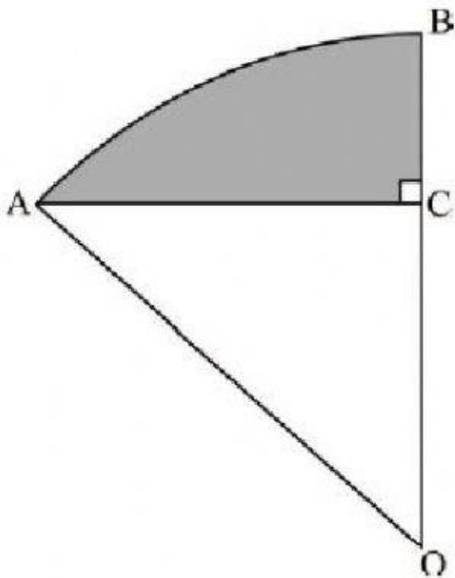


**QUESTION 5**

The diagram shows an arc, AB, of a circle with centre O and radius  $r$ . The line AC is drawn perpendicular to the line OCB. The region bounded by AC, BC and arc AB is shaded.  $\widehat{AOB} = \frac{\pi}{6}$  radians.



5.1 Find the area of  $\Delta AOC$ , in terms of  $r$ . (6)

$$\boxed{\phantom{000000}} = \frac{1}{2} r^2 \left( \frac{\pi}{6} \right)$$

$$= \frac{\pi r^2}{6}$$

$$\boxed{\phantom{000000}}$$

5.3 If the shaded area is  $\frac{2\pi - 3\sqrt{3}}{6}$   $\text{cm}^2$ , calculate the value of  $r$ . (6)  
[16]

$$\boxed{\phantom{000000}} = \frac{\pi r^2}{6} - \frac{\sqrt{3} r^2}{2} = \frac{2\pi - 3\sqrt{3}}{6}$$

$$\therefore 2\pi r^2 - 3\sqrt{3} r^2 = 8\pi - 12\sqrt{3}$$

$$\therefore r^2 = 4 \text{ i.e. } r = 2$$

5.2 Find the area of the sector OAB, in terms of  $r$ . (4)

$$\boxed{\phantom{000000}} = \frac{1}{2}r^2 \left(\frac{\pi}{6}\right)$$

$$= \frac{\pi r^2}{6}$$

$$\boxed{\phantom{000000}}$$

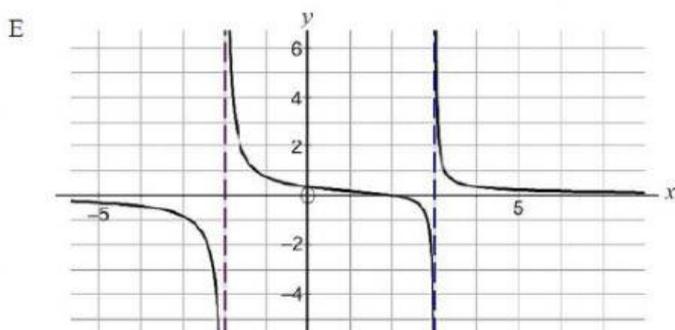
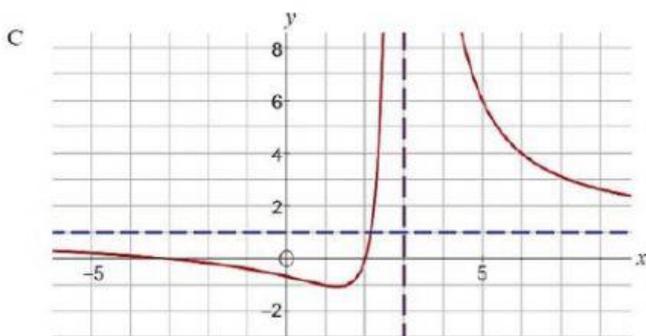
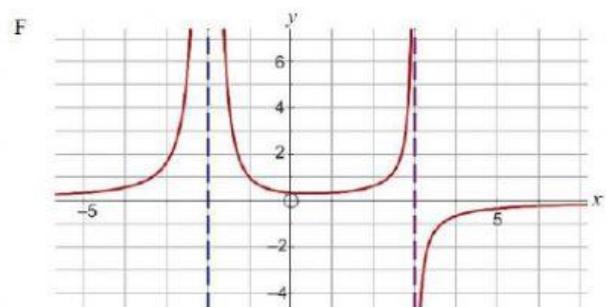
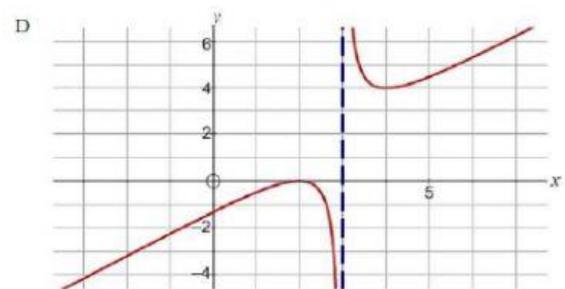
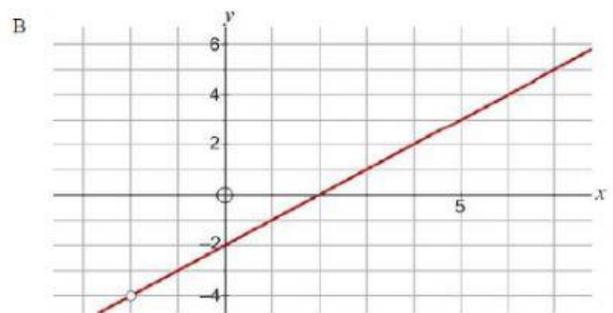
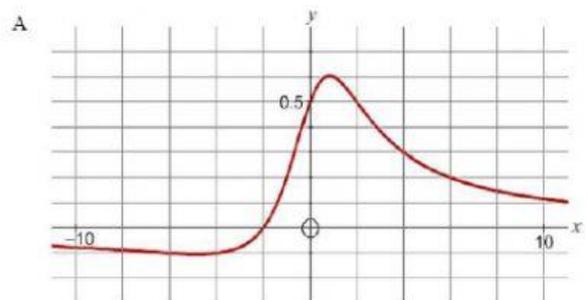
Match the following rational functions to the appropriate graphs, A–F, below:

6.1  $f(x) = \frac{x^2-4}{x+2}$

6.2  $f(x) = \frac{x-2}{x^2-x-6}$

6.3  $f(x) = \frac{x^2+x-6}{x^2-6x+9}$

6.4  $f(x) = \frac{x^2-4x+4}{x-3}$



### QUESTION 7

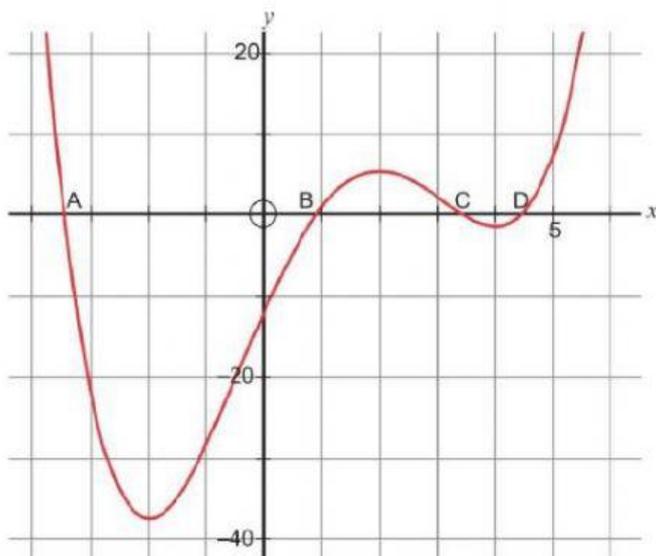
Find the equation of the tangent to the curve  $x^3 - 2y^2 = 14 - 4x$  at the point (2; 1).

[11]

$$3x^2 - 4y \cdot \frac{dy}{dx} = -4$$
$$\therefore \frac{dy}{dx} = \frac{3x^2 + 4}{4y}$$
$$\therefore \frac{dy}{dx} = 4$$

### QUESTION 8

The graph of  $f(x) = \frac{1}{4}x^4 - \frac{4}{3}x^3 - 2x^2 + 16x - 12$  is shown, with stationary points at  $x = -2$ ,  $x = 2$  and  $x = 4$ . The graph has  $x$ -intercepts at the points indicated by A, B, C and D.



- 8.1 Without first solving the equation, state with clear justification which of the intercepts, A, B, C or D, will be found using Newton's method with an initial approximation of  $x_0 = 2,1$ .

(3)

8.2 State any restrictions on the initial approximation of  $x$ .

(2)

8.3 Given  $x_0 = 3$ , determine the  $x$ -intercept at C, correct to 6 decimal places.

(8)  
[13]

$$x_{r+1} = x_r - \frac{\frac{1}{3}x^4 - \frac{4}{3}x^3 - 2x^2 + 16x - 12}{x^3 - 4x^2 - 4x + 16}$$

$x_0$

$x_1$

$x_2 =$

$x_3 =$

### QUESTION 9

A function is given as  $f(x) = x + 4(x + 1)^{-2}$

9.1 Determine the coordinates of the stationary point and prove that this is a local minimum.

(10)

$f'(x) =$

$1 - \frac{8}{(x+1)^3}$

$\therefore x + 1 = 2$    
 $\therefore x = 1$  and

$f''(x) =$

$\therefore f''(1) = \frac{3}{2} > 0$

