

$$f(x) = \begin{cases} \frac{x^2}{18} & , -3 < x < 3 \\ 0 & , \text{otherwise} \end{cases}$$

For  $x \leq -3$

$$F(x) = 0 = 0$$

For  $-3 < x < 3$

$$F(x) = 0 + \int_{-3}^x \frac{t^2}{18} dt$$

$$= 0 + \left[ \frac{t^3}{54} \right]_{-3}^x$$

$$= \frac{x^3}{54} - \left( \frac{-1}{2} \right)$$

$$= \frac{x^3}{54} + \frac{1}{2}$$

For  $x \geq 3$

$$F(x) = \frac{1}{2} + \int_3^x 0 dt$$

$$= \frac{1}{2} + \frac{1}{2} + 0$$

$$= 1$$

$$F(x) = \begin{cases} 0 & , x \leq -3 \\ \frac{x^3}{54} + \frac{1}{2} & , -3 < x < 3 \\ 1 & , x \geq 3 \end{cases}$$

$x \leq -3$
$F(-3)$
$\int_{-\infty}^x 0 dt$
$-3 < x < 3$
$\left[ \frac{t^3}{54} \right]_{-3}^x$
$F(3)$
$\int_{-3}^x \frac{t^2}{18} dt$
$\frac{x^3}{54} + \frac{1}{2}$
$x \geq 3$
$\int_3^x 0 dt$

For  $x < 0$   
 $F(x) = 0$

For  $0 \leq x < 1$   
 $F(x) = 0 + \int_0^x \frac{1}{4} dt$   
 $= 0 + \left[ \frac{t}{4} \right]_0^x$   
 $= \frac{x}{4}$

For  $1 \leq x < 3$   
 $F(x) = \frac{1}{4} + \int_1^x \frac{3}{8}(3-t) dt$   
 $= \frac{1}{4} + \left[ \frac{3}{8} \left( 3t - \frac{t^2}{2} \right) \right]_1^x$   
 $= \frac{1}{4} + \frac{9x}{8} - \frac{3x^2}{16} - \frac{15}{16}$

For  $x \geq 3$   
 $F(x) = \frac{-3x^2}{16} + \frac{9x}{8} - \frac{11}{16} + \int_3^x 0 dt$   
 $= \frac{-3x^2}{16} + \frac{9x}{8} - \frac{11}{16} + 0$

$\therefore F(x) = \begin{cases} 0 & , x < 0 \\ \frac{x}{4} & , 0 \leq x < 1 \\ \frac{-3x^2}{16} + \frac{9x}{8} - \frac{11}{16} & , 1 \leq x < 3 \\ 1 & , x \geq 3 \end{cases}$

$$f(x) = \begin{cases} \frac{1}{4} & , 0 \leq x < 1 \\ \frac{3}{8}(3-x) & , 1 \leq x \leq 3 \\ 0 & , \text{otherwise} \end{cases}$$

$\int_{-\infty}^x 0 dt$
$F(0)$
1
$x < 0$
$\int_1^x \frac{3}{8}(3-t) dt$
$\frac{x}{4}$
$\frac{3}{8} \left[ 3t - \frac{t^2}{2} \right]_1^x$
$\left[ \frac{t}{4} \right]_0^x$
$\int_0^x \frac{1}{4} dt$
$F(1)$
$F(3)$
$\frac{-3x^2}{16} + \frac{9x}{8} - \frac{11}{16}$
$\int_3^x 0 dt$
$x \geq 3$
0