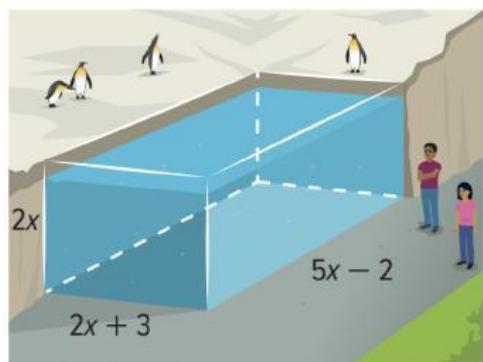


**ANIMALS** For an exhibit with six or fewer Emperor penguins, the pool must have a depth of at least 4 feet and a volume of at least 1620 gallons, or about  $217 \text{ ft}^3$ , per bird. If a zoo has five Emperor penguins, what should the dimensions of the pool shown at the right be to meet the minimum requirements?



### Part A Write a polynomial equation.

Use the formula for the volume of a rectangular prism,  $V = \ellwh$ , to write a polynomial equation that represents the volume of the pool. Let  $h$  represent the depth of the pool.

Since the minimum required volume for the pool is  $217 \text{ ft}^3$  per penguin, or  $217 \cdot 5 = 1085 \text{ ft}^3$ , the equation that represents the volume of the pool is  $(2x + 3)(5x - 2)2x = 1085$ . Simplify the equation.

$$(2x + 3)(5x - 2)2x = 1085 \quad \text{Volume of pool}$$

$$[2x(5x) + 2x(-2) + 3(5x) + 3(-2)]2x = 1085 \quad \text{FOIL}$$

$$(10x^2 - 4x + 15x - 6)2x = 1085 \quad \text{Simplify.}$$

$$(10x^2 + 11x - 6)2x = 1085 \quad \text{Combine like terms.}$$

$$20x^3 + 22x^2 - 12x = 1085 \quad \text{Distributive Property}$$

So, the volume of the pool is  $20x^3 + 22x^2 - 12x = 1085$ .

### Part B Write and solve a system of equations.

Set each side equal to  $y$  to create a system of equations.

$$y = 20x^3 + 22x^2 - 12x \quad \text{First equation}$$

$$y = 1085 \quad \text{Second equation}$$

Enter the equations in the **Y =** list and graph.

Use the **intersect** feature on the **CALC** menu to find the coordinates of the point of intersection.

The real solution is the  $x$ -coordinate of the intersection, which is

### Part C Find the dimensions.

Substitute 3.5 feet for  $x$  in the length, width, and depth of the pool.

$$\text{Length: } 2x + 3 = \boxed{\phantom{00}} \quad \text{Width: } 5x - 2 = \boxed{\phantom{00}}$$

$$\text{Depth: } 2x = \boxed{\phantom{00}}$$